

L# 19

Lecture schedule : 04/23 }
 04/25 } read 2.1.1 to 2.1.5 in Roger Kamm's manuscript

04/30 read 2.2.1 to 2.2.6

05/05 Peter So : guest lecturer

05/07 read 2.1.6

- Work done by a sarcomere : $\sigma A l = \int_{-\infty}^{+\infty} n(x) \beta_s \frac{A_s}{2} K x dx$

σ stress

A cross-sectional area of sarcomere

l contraction length / distance between binding sites (during one cycle, only one cross-bridge can form)

n(x) probability of binding

β_s number of sarcomeres per unit volume

$\frac{A_s}{2}$ area of half a sarcomere (symmetry)



* length of a sarcomere

Kx spring force

Typical numbers $v_{max} \approx 6 \mu\text{m.s}^{-1}$, $h \approx 4 \text{ nm}$, $k_e^0 \approx 2000 \text{ N}^{-1}$, $F_{max} \approx 1 \text{ pN}$

■ Goals : why is cell mechanics important?

important components of the cell

plasma membrane (biophysics today studies structural components one by one)

■ Plasma membrane

reference : Israelachvili "Intermolecular & surface forces"

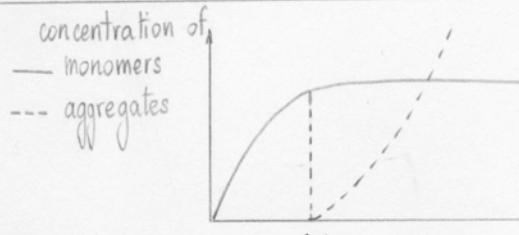
- self assembly of amphiphiles (= amphipathic = tolerant of both)



1- at what concentration do structures form?

2- geometry of structures?

■ Critical micelle concentration CMC



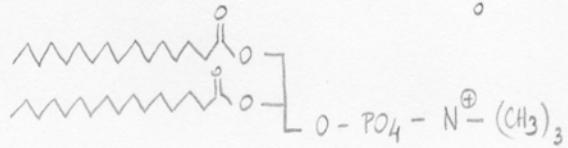
total concentration
of surfactant (amphiphile)

qualitatively, as hydrophobicity ↑, CMC ↓
compare common soap (sodium stearate)

phospholipids (DPPC)



1 head 1 tail CMC ~ 1 mM



1 head 2 tails CMC ~ 10^-9 M

Competing forces : - attractive : hydrophobic tails
- repulsive : hydrophilic tails
ionic groups
steric repulsion

- Micelles / aggregates are dynamic



Typical resonance time (stay in aggregate state)

single tail	$\tau_R \sim 10^{-4} s$
double tail	$\tau_R \sim 10^4 s$

Geometry of structure

geometric packing

3 parameters

a_0 optimal head area

v volume of hydrocarbon tail

l_c length scale & contour length of tail

shape factor $\frac{v}{a_0 l_c}$