1.033/1.57 H#1: Deformation & Strain

Due: September 17, 2003

MIT – 1.033/1.57 Fall 2003 Instructor: Franz-Josef ULM

DOUBLE SHEAR: We consider a double shear test on a material specimen as sketched in the Figure below. The displacement field is defined by:

$$\underline{\xi} = \alpha \left(X_2 \underline{e}_1 + X_1 \underline{e}_2 \right); \quad \alpha \ge 0$$

Determine

1. In Finite Deformation:

- (a) The deformation gradient;
- (b) The change in volume of the material specimen;
- (c) The change in surface area and orientation of any surface oriented by $N = 1/\sqrt{2} (e_1 + e_2)$. How does the result compare to the simple shear scenario (see lecture Notes #1.6)
- (d) The Green-Lagrange Strain Tensor, its Eigenvalues and Egenvectors (i.e. principal strains and principal strain directions)
- (e) The linear dilatations and distortions.

2. In Infinitesimal Deformation:

- (a) How does the assumption of infinitesimal deformation read in double shear?
- (b) How do the elements determined in Part 1 change in the infinitesimal deformation tehory?



Figure 1: