

Ite	m	Profit	Weight
	0	0	C
	1	11	1
	2	21	11
	3	31	21
	4	33	23
	5	43	33
	6	53	43
	7	55	45
	8	65	55

Γ

• Item 0 is sentinel, needed in branch-and-bound too

KnapsackBB constructor				
<pre>public class KnapsackBB { private DPltem[] items; private int capacity; private int[] x; private int[] y; // We private double solutionProfi private double currWgt; private double currProfit; private double newWgt; private int k; private int partItem;</pre>	<pre>// Input list of items // Max weight allowed in knapsack // Best solution array: item i in if xi=1 orking solution array at current tree node t= -1; // Profit of best solution so far // Weight of solution at this tree node // Profit of solution at this tree node // Weight of solution from bound() method // Profit of solution from bound() method // Level of tree in knapsack() method // Level of tree in bound() method</pre>			
<pre>public KnapsackBB(DPItem[] i items= i; capacity= c; x= new int[items.length y= new int[items.length }</pre>	, int c) {];];			

KnapsackBB knapsack()					
public void knapsack() {					
int n= items.length; // Nu	umber of items in problem				
do { // Wi	nile upper bound < known soln,backtrack				
while (bound() <= solutionProfit) {					
while (k != 0 && y[k] != 1)	<pre>// Back up while item k not in sack</pre>				
k;	<pre>// to find last object in knapsack</pre>				
if (k == 0)	// If at root, we're done. Return.				
return;					
y[k]= 0;	// Else take k out of soln (R branch)				
currWgt -= items[k].weight;	// Reduce soln wgt by k's wgt				
currProfit -= items[k].profi	t; // Reduce soln profit by k's prof				
}	<pre>// Back to while(), recompute bound</pre>				
currWgt= newWgt;	// Reach here if bound> soln profit				
currProfit= newProfit;	// and we may have new soln.				
k= partitem;	// Set tree level k to last, possibly				
	// partial item in greedy solution				
if (k == n) {	// If we've reached leaf node, have				
sol uti onProfi t= currProfi t;	// actual soln, not just bound				
System.arraycopy(y, 0, x, 0,	y.length); // Copy soln into array x				
k= n-1; // Back up to prev	tree level, which may leave solution				
} el se	// Else not at leaf, just have bound				
y[κ]= 0;	// lake last item k out of soln				
<pre>} while (true);</pre>	// Infinite loop til backtrack to k=0				

KnapsackBB bound()					
<pre>private double bound() {</pre>					
bool ean found= fal se;	// Was bound found?L.e.,is last item partial				
double boundVal = -1;	// Value of upper bound				
int n= items.length;	// Number of items in problem				
newProfit= currProfit; newWgt= currWgt;	// Set new prof as current prof at this node				
partItem= k+1;	// Go to next lower level, try to put in soln				
while (partItem < n && !	found) { // More items & haven't found partial				
if (newWgt + items[partItem].weight <= capacity) { // If fits					
newWgt += items[partItem].weight; // Update new wgt, prof					
newProfit += items[p	artItem].profit; // by adding item wgt,prof				
y[partItem]= 1;	// Update curr soln to show item k is in it				
} el se {	// Current item only fits partially				
boundVal = newProfit + (capacity -					
<pre>newWgt)*items[partItem].profit/Items[partItem].weight;</pre>					
found= true; }	<pre>// Compute upper bound based on partial fit</pre>				
partltem++;	<pre>// Go to next item and try to put in sack</pre>				
}					
if (found) { // If	we have fractional soln for last item in sack				
partItem; // Ba	ck up to prev item, which is fully in sack				
return boundVal; // Re	turn the upper bound				
} el se {					
return newProfit;// Re	turn profit including last item				

```
KnapsackBB main()
   public static void main(String[] args) {
       // Sentinel - must be in 0 position even after sort
       DPItem[] list= {new DPItem(0, 0),
                       new DPI tem(11, 1),
                       new DPI tem(21, 11),
                       new DPI tem(31, 21),
                       new DPI tem(33, 23),
                       new DPI tem(43, 33),
                       new DPI tem(53, 43),
                       new DPItem(55, 45),
                       new DPItem(65, 55),
       };
       Arrays.sort(list, 1, list.length);
                                              // Leave sentinel in 0
       int capacity= 110;
       // Assume all item weights <= capacity. Not checked. Discard
       // Assume all item profits > 0. Not checked. Discard.
       KnapsackBB knap= new KnapsackBB(list, capacity);
       knap. knapsack();
       knap. outputSol uti on();
   }
}
// main() almost identical to DPKnap.
// DPItem identical, outputSolution() almost identical to DP code
```


Next time

- Breadth first search in branch and bound trees
- Fixed facility location problem
 - Mixed integer problem
 - Uses linear program (LP) as subproblem
 - We solve the LP with a shortest path algorithm!
- The depth first search for the knapsack problem is mostly pedagogical
 - Sometimes depth first search works well enough for your particular problem and data
 - Usually you need to be a bit more sophisticated

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