6.837 Introduction to Computer Graphics Final Exam Tuesday, December 20, 2011 9:05-12pm Two hand-written sheet of notes (4 pages) allowed

NAME:

1	/ 17
2	/ 12
3	/ 35
4	/ 8
5	/ 18
Total	/ 90

ſ

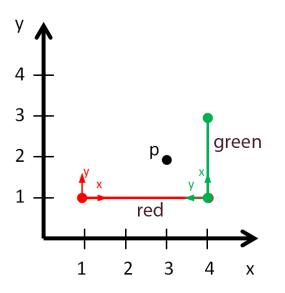
/17]

1 SSD

In this problem we are going to animate a simple character using linear blend skinning.

1.1 Computing Bind Pose

We are given a skeleton and a skin mesh in a bind pose. Our character has only two bones (red and green) and we are interested in only one mesh vertex, p. See the diagram below.

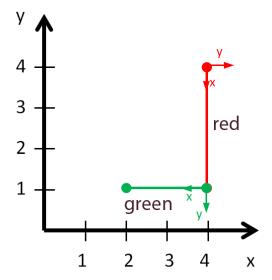


Compute rigid-transformation matrices \mathbf{B}_{red} and \mathbf{B}_{green} that transform mesh vertices from local bone coordinate system to the global coordinate system. [/4]

Then compute \mathbf{p}_{red} and \mathbf{p}_{green} , the bone space coordinates of vertex \mathbf{p} relative to the red and green bones, either geometrically or by inverting \mathbf{B}_{red} and \mathbf{B}_{green} . [/4]

1.2 Bone Transformations

We have transformed each bone of this character according to the diagram below.



Compute matrices \mathbf{T}_{red} and \mathbf{T}_{green} that transform mesh vertices from local bone coordinate system to the global coordinate system. [/4]

1.3 Computing Vertex Positions

Using previously computed \mathbf{p}_{red} and \mathbf{p}_{green} and the new bone matrices \mathbf{T}_{red} and \mathbf{T}_{green} , determine the transformed positions of vertex \mathbf{p} in the global coordinate system, both for the red and green bone.

[/4]

Given that the weights for the red and green bone are 0.5, compute the final transformed vertex position in the global coordinate system. [/1]

2 Shading

[

Suppose we have a sphere centered at the origin, $x^2 + y^2 + z^2 = r^2$. There is a light source at (a,b,c). Generate a formula for finding the color at any point (x,y,z) on the surface of the sphere, assuming that there is diffuse reflection. Define any additional terms you introduce. [/12]

3 Ray Tracing

3.1 Refraction

Recall that the formula for the outgoing angle of a refracted ray is:

$$T = \left[\eta_r(N \cdot I) - \sqrt{1 - \eta_r(1 - (N \cdot I)^2)}\right]N - \eta_r I$$

What is the name of the physical phenomenon that causes the term under the square root to be negative? [/3]

How should we deal with the transmitted ray in such a case? [/3]

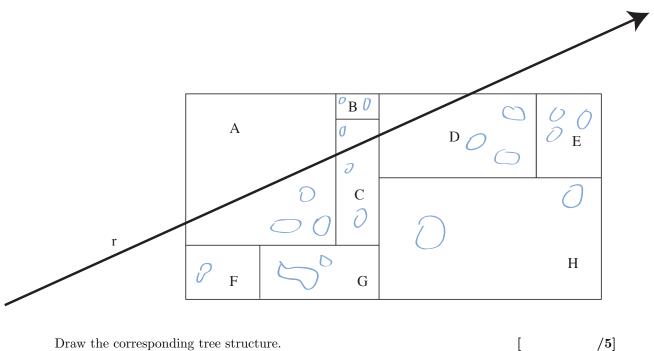
$$\begin{bmatrix} & /35 \end{bmatrix}$$

3.2Kd-tree

/13]

ſ

Below is the representation of a given 2D Kd-tree with the leaves indicated by upper-case letters. We have drawn some leaf geometry in blue for motivation, but you do not need to consider it, albeit to notice that the particular ray r does not have any intersection with the scene.



Draw the corresponding tree structure.

/5]

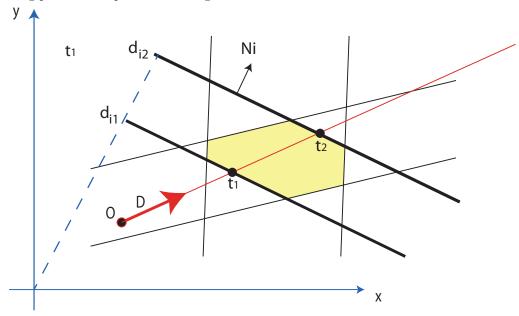
We now consider the traversal of this kd-tree for the ray r, as it would happen for ray-tracing acceleration. For warm up, draw the four intersections with the sides of the bounding box of the tree that occur during the initialization of the traversal. ſ /2]

We now want you to show the order in which ray-plane intersections are computed for the efficient hierarchical traversal of the tree. Draw a cross at each intersection point and write its order as a number next to it. NB: we want the order in which intersections are calculated, not the order along the ray. Make sure you use a smart traversal that only visits relevant nodes and that the order can enable early termination if appropriate. **/6**] ſ

3.3 Ray slab intersection

ſ

We seek to compute the intersection between a ray and a convex object defined as the intersection of a set of slabs. Slabs are the space between two parallel planes (see figure). A slab with index *i* is defined by a normal N_i and two real numbers d_{i1} and d_{i2} . The axis-aligned bounding boxes we studied in class are a special type of such objects where the three slabs have axis-aligned normals. We want to adapt the fast ray-box intersection algorithm to handle general slabs. We parameterize our ray as P(t) = O + tD where O is the origin and D the direction. You can assume that the ray is going in the positive direction (i.e. t_1 is always smaller than t_2) and you should not worry about the ray being parallel to a plane or starting inside the slab.



First, we consider a single slab with index *i*. Write the equation for t_1 and t_2 , the intersection parameters for the first and second plane delimiting this slab. [/6]

We now turn to the intersection of the ray and the CSG intersection of N slabs. We initialize t_{start} and t_{end} with the values for t_1 and t_2 given by the first pair of planes. Write pseudocode to update t_{start} and t_{end} with the values t'_1 and t'_2 for a new pair of planes. [/6]

Finally, after they have been updated to take into account all slabs, give a criterion on t_{start} and t_{end} that determines if the intersection between the ray and the volume is non-empty. Do not worry about whether the slab is in front or behind the origin.

[/4]

4 Rasterization

/8]

[

We want to implement two-scale rasterization where rectangular groups of pixels are quickly declared fully inside or fully outside a triangle. Assume you are given the three edge equations so that a 2D point P inside the triangle respects $P \cdot N_i - d_i > 0$ for i = 0..2. A rectangular region is described by its four corners P_j for j = 0..3.

What is the condition for the full rectangle to be entirely inside the triangle? [/4]

Things are more tricky for the test to be fully outside. A naïve solution would be to say that all four corners fail the edge tests. Find a counter example. [/4]

5	Graphics hardware	[/18]
List	one form of task vs. data parallelism in graphics hardware.]	/4]

Example of task parallelism:

Example of data parallelism:

Attribute the following properties to either graphics hardware or CPU (we recommend against using the acronym GPU because we might have a hard time distinguishing your Gs and Cs :-([/6]

- optimized for latency

- latency hiding

- extremely long pipeline (1000 stages)

Would the following algorithm be implemented in a vertex or pixel shader? [/8]

SSD skinning

Phong shading

Blend shapes

Shadow map query

6.837 Computer Graphics Ø

For information about citing these materials or our Terms of Use, visit: http://ocw.mit.edu/terms.