6.895 Theory of Parallel Systems

Due: Monday, September 22nd

Problems 1–3

**Problem 1.** (Exercise 1-3 from Minicourse on Multithreaded Programming) Prove that a greedy scheduler achieves the stronger bound:

$$T_P \le \frac{(T_1 - T_\infty)}{P} + T_\infty \,. \tag{1}$$

**Problem 2.** (Exercise 1-6 from Minicourse on Multithreaded Programming) Professor Tweed takes some measurements of his (deterministic) multithreaded program, which is scheduled using a greedy scheduler, and finds that  $T_4 = 80$  seconds and  $T_{64} = 10$  seconds. What is the fastest that the professor's computation could possibly run on 10 processors?

**Problem 3.** (Different Speed Processors) In this problem we consider how to schedule on processors of different speeds. Let there be p processors  $1 \dots p$ , where processor i has speed  $\pi_i$  steps/time. Assume that  $\pi_1 \ge \pi_2 \ge \dots \ge \pi_p$ . Let  $W_1$  represent the *total work*, that is the total number of nodes in the dag G. Let  $W_{\infty}$  represent the *critical path length* of the graph, that is, the number of nodes in the longest chain in G. Let  $\pi_{ave}$  steps/time be the *average speed* of the processors, that is,  $\pi_{ave} = \sum_{i=1}^{p} \pi_i / p$ . Let  $T_p$  represent the *optimal time* to execute G on p processors.

**Problem 3.a.** Briefly explain why an arbitrary greedy schedule may perform poorly.

**Problem 3.b.** Describe a good greedy scheduler for this system.

**Problem 3.c.** Prove an analog of Graham/Brent for your scheduler. You should be able to show that:

$$T_p \leq \frac{W_1}{p \pi_{ave}} + \left(\frac{p-1}{p}\right) \frac{W_{\infty}}{\pi_{ave}} \,. \tag{2}$$

**Problem 3.d.** Can you still show that the time to complete all tasks is within a factor of 2 of optimal? Why or why not?