Logic I Fall 2009 Quiz 4

Complete the definitions below.

- 1. **P** is derivable from  $\Gamma$  ( $\Gamma \vdash \mathbf{P}$ ) iff...
- 2. **P** is truth-functionally entailed by  $\Gamma$  ( $\Gamma \vDash \mathbf{P}$ ) iff...
- 3.  $\Gamma$  is truth-functionally consistent iff...
- 4.  $\Gamma$  is maximally consistent in SD iff...

We can prove by mathematical induction that for any sentence  $\mathbf{P}$  of SL, on any TVA  $\mathbf{P}$  has the same truth-value as  $\mathbf{P}$  prefixed by any even number of negations. Complete the following proof, letting S be the ordered sequence of all non-negative even integers (this includes 0).

Basis Clause: ...

**Inductive Step:** If, for the ith member of S, on any TVA **P** has the same truth-value as **P** prefixed by n negation symbols, where n is the ith member of S, then ...

Proof of inductive step: ...

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