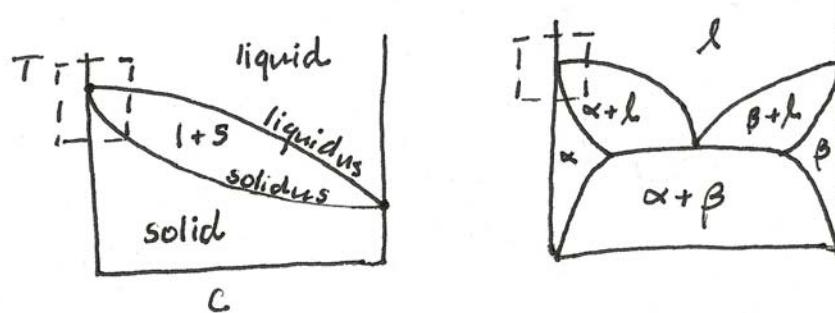


## 3.044 MATERIALS PROCESSING

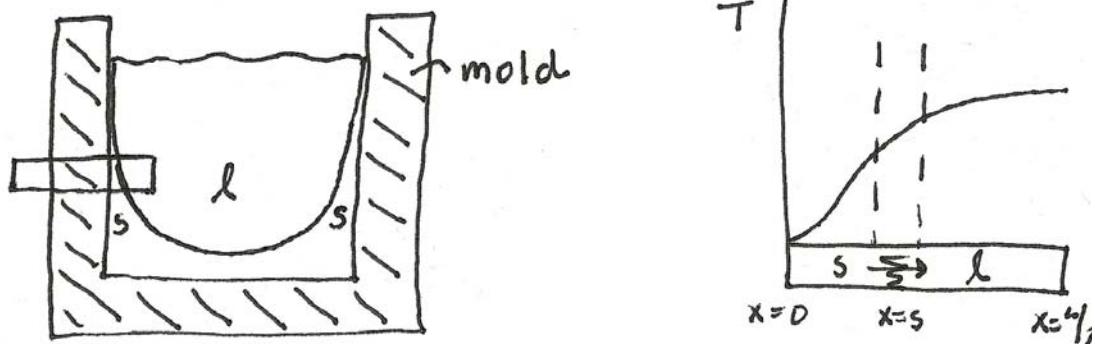
### LECTURE 11

#### Solidification of Multicomponent Liquids



single component system: single  $T_m$

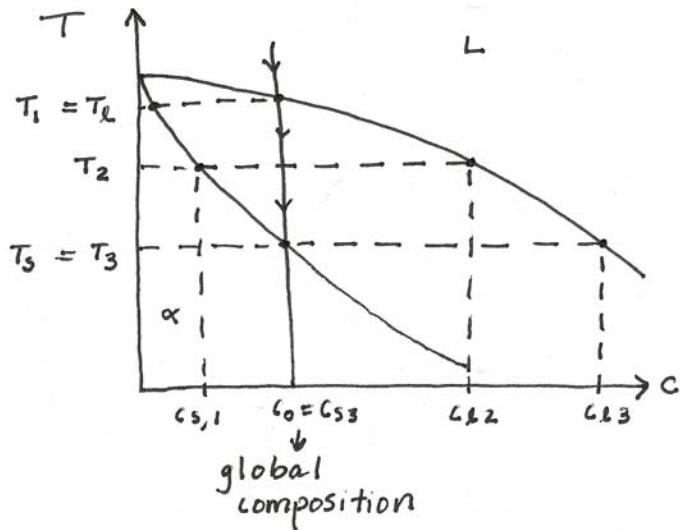
multicomponent system: solidify over a range of  $T$



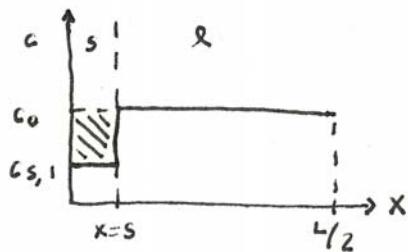

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Date: March 19th, 2012.

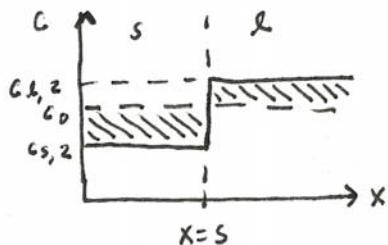
1. **Assume:** equilibrium solidification (rapid diffusion in both liquid and solid)



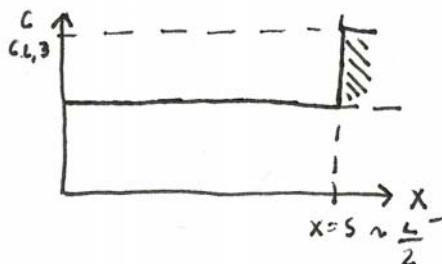
@  $T = T_1 = T_L$



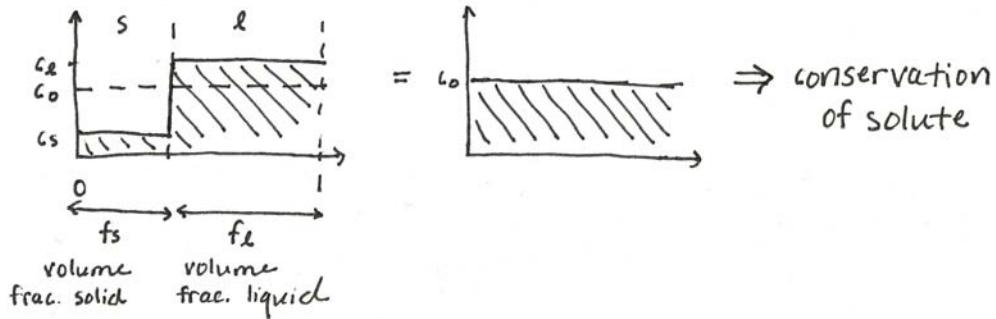
@  $T_2$



@  $T_3 = T_S$



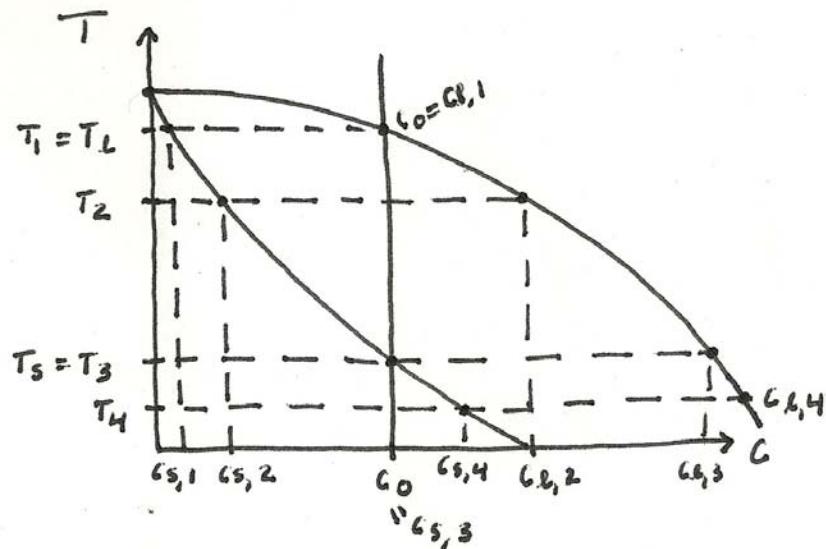
At any time:

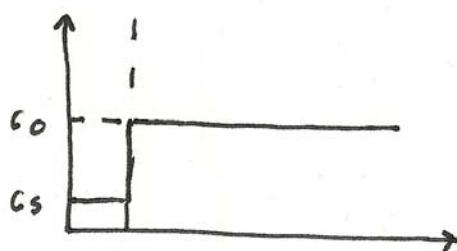
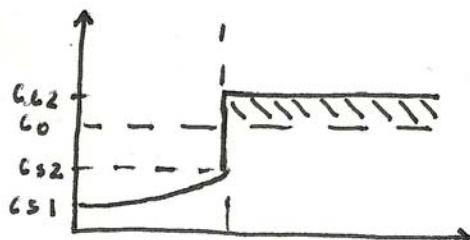
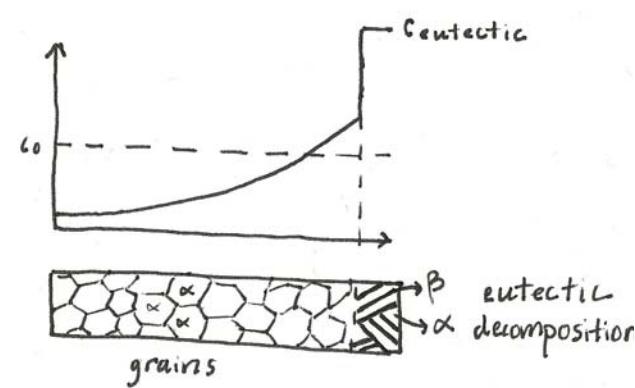
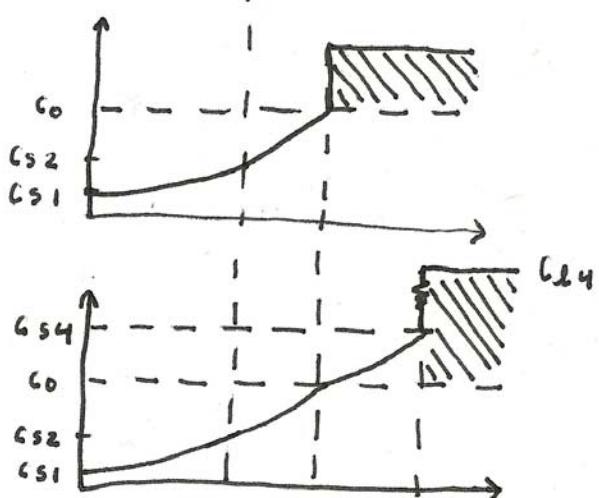


Key Lesson: phase transformations push solute around

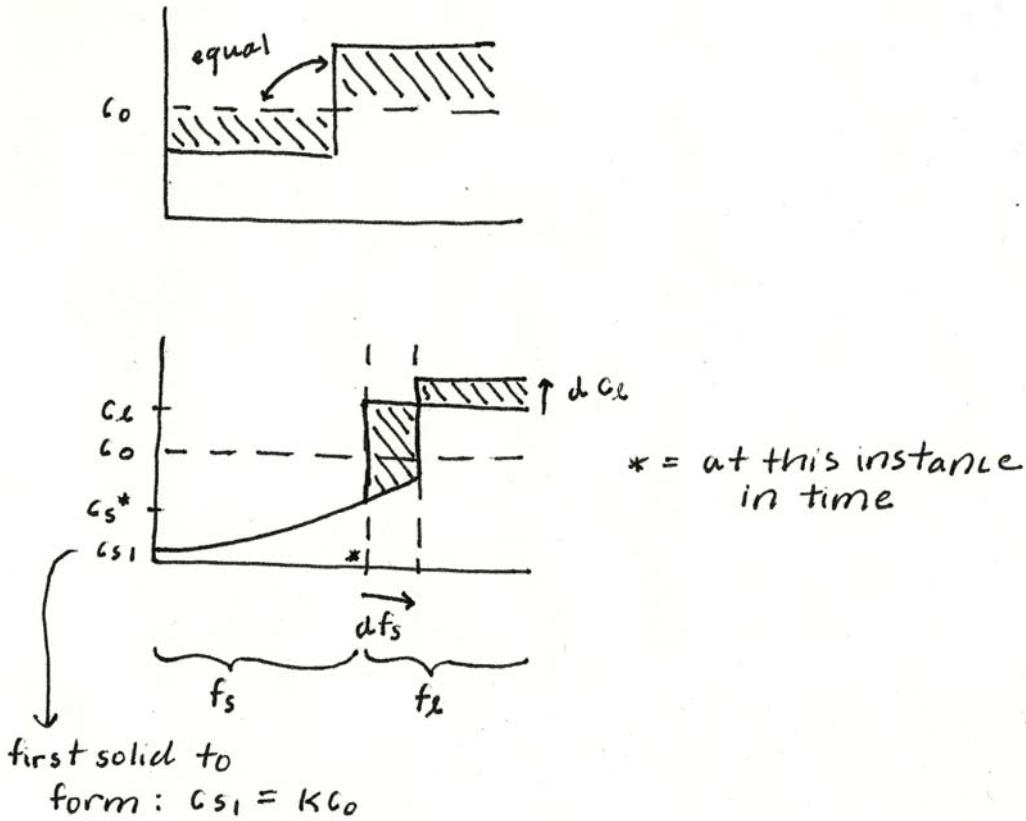
Conservation of Solute: **Lever Rule:**  $c_0 = f_s \cdot c_s + f_l \cdot c_l$

**More realistic assumption:** diffusion is fast in liquid and non-existent in solid



$\text{@ } T_1$  $\text{@ } T_2$  $\text{@ } T_3$ 

Solute Balance:



$$(c_l - c_s^*) df_s = f_l \cdot dc_l$$

$$(c_l - c_s^*) df_s = (1 - f_s) \cdot dc_l$$

$$\frac{df_s}{1 - f_s} = \frac{dc_l}{c_l - c_s^*}$$

B.C.

 @  $f_s = 0 : c_l = c_0 \text{ & } c_s^* = c_{s,1}$

Define **k**: partition coefficient

$$k = \frac{c_s}{c_l}$$

- from phase diagram, k describes the width of a 2-phase field
- k is a materials constant if and only if the solidus and liquidus are lines
- first solid to form is of composition  $c_{s,1}$

$$c_{s,1} = kc_0$$

$$c_s^* = c_{s,1} = kc_0$$

Solve: Non-Equilibrium Lever Rule

$$c_S^* = kc_0(1 - f_s)^{(k-1)} \quad \text{or} \quad c_l = c_0 f_l^{(k-1)}$$

⇒ The Non-Equilibrium Lever Rule applies to stirred liquids, rapid diffusion in liquid, slow solid diffusion

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3.044 Materials Processing  
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