## 8.851 Homework 7

Iain Stewart, April 2, 2003 (due Apr.9)

## Problem 1) Chiral Perturbation Theory and Decay Constants

a) Work out the tree level Feynman rules for the four meson interactions with SU(3) chiral perturbation theory and the leading order Lagrangian. (Use the octet basis  $M = \pi^a \lambda^a / \sqrt{2}$  rather than the charged particle basis.)

b) Work out the tree level Feynman rules in chiral perturbation theory for the left-handed SU(3) octet current  $(\bar{\psi}\gamma^{\mu}P_L\lambda^a\psi)$  with one and three external mesons.

c) Write down the loop diagrams and terms in the chiral Lagrangian that are needed to give the decays constants at order  $p^4$  (where  $p \sim m_{\pi} \sim m_K$  so this also means order  $m_{\pi}^4 \sim m_q^2$  etc.).

d) Determine the explicit contribution of the order  $p^4$  Lagrangian terms to  $f_{\pi}$  and  $f_K$  taking  $m_u = m_d = \hat{m}$ , but  $\hat{m} \neq m_s$ .

e) Calculate the loops in part c) using dimensional regularization. Combine your result with d) to derive the full expression for  $f_{\pi}$  and  $f_K/f_{\pi}$  at this order (still taking the isospin limit  $m_u = m_d$ ).

f) Extract a value for the relevant low energy contants,  $L_i$ , using the data  $f_K/f_{\pi} = 1.23 \pm .02$ , and discuss whether your result agrees with naive dimensional analysis.